

Week 3 Problem Set

Problem 1

Consider a block of a single tissue type placed in the a 3T human MRI scanner.

Problem 1a A time  $t = 0$  an initial magnetization  $M_0\hat{z}$  points along the direction ( $\hat{z}$ ) of the main magnetic field  $\mathbf{B}_0 = B_0\hat{z}$ .

1. What is the Larmor frequency  $\omega$  in terms of the main field  $B_0$ ?
2. What is the longitudinal magnetization  $m_{\parallel}$  at  $t = 0$  ?
3. What is the transverse magnetization  $m_{\perp}$  at  $t = 0$  ?

Problem 1b An excitation pulse of  $90^\circ$  is applied along the  $x$ -axis at time  $t = 0$ . Assuming that this pulse happens instantly. Ignore  $T_1$  relaxation.

1. What is the transverse magnetization  $m_{\perp}$  at a time  $t = \tau$  shortly (a few ms) after the pulse?
2. A series of refocussing ( $180^\circ$ ) pulses are applied. Assume an echo occurs at the time  $\tau_E$ . What is the amplitude of this echo?
3. Why is  $T_2^*$  refocussed but  $T_2$  isn't?

Problem 2

Consider a normal human brain in the a 3T human MRI scanner.

Problem 2a The MRI signal is

$$s(\mathbf{k}) = \int m_{\perp}(\mathbf{x}, t) e^{-i\mathbf{k} \cdot \mathbf{x}} d\mathbf{x} \quad (1)$$

1. What is  $i$ ?
2. What is  $\mathbf{k}$ ?
3. What is  $\mathbf{x}$ ?
4. What is the “ $\cdot$ ” between  $\mathbf{k}$  and  $\mathbf{x}$ ?

Problem 2b

We apply gradients  $G_x$ ,  $G_y$  and  $G_z$  along each of the three axes  $x$ ,  $y$ , and  $z$ , respectively, for a time  $\tau$ .

1. Write the gradients in vector form
2. Write the spatial coordinates in vector form
3. What is  $\mathbf{k} \cdot \mathbf{x}$ ?

Problem 2c

The applied gradients are  $G_x = 1G/cm$ ,  $G_y = 1G/cm$  and  $G_z = 0G/cm$ .

1. What is the angle of phase generated in the  $xy$  plane by these gradients?

2. What is the angle of phase generated in the  $xy$  plane if we double the strength of  $G_x$ ?
3. What is the angle of phase generated in the  $xy$  plane if we half the strength of  $G_y$ ?